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Information technology - Language independent arithmetic - Part 3: Complex integer and floating point arithmeti c and complex elementary numerical functions

Contents

Page

Foreword vii Introduction viii 1 Scope 1 1.1 Inclusions 1

1.2 Exclusions 2

2 Conformity 3 3 Normative references 4 4 Symbols and definitions 4 4.1 Symbols 4

4.1.1 Sets and intervals 4
4.1.2 Operators and relations 4
4.1.3 Mathematical functions 5
4.1.4 Exceptional values 6
4.1.5 Datatypes and special values 6
4.1.6 Complex value constructors and complex datatype constructors 8
4.2 Definitions of terms 9

5 Specifications for imaginary and complex datatypes and operations 14 5.1 Imaginary and complex integer datatypes and operations 14
5.1.1 The complex integer result helper function 15
5.1.2 Imaginary and complex integer operations 15
5.1.2.1 Complex integer comparisons 15
5.1.2.2 Multiplication by the imaginary unit 17
5.1.2.3 The real and imaginary parts of a complex value 17
5.1.2.4 Formation of a complex integer from two real valued integers 18
5.1.2.5 Basic complex integer arithmetic 18
5.1.2.6 Absolute value and signum of integers and imaginary integers 21
5.1.2.7 Divisibility interrogation 21
5.1.2.8 Integer division and remainder extended to imaginary and complex integers 22
5.1.2.9 Maximum and minimum 27
5.2 Imaginary and complex floating point datatypes and operations 28
5.2.1 Maximum error requirements 28
5.2.2 Sign requirements 29
5.2.3 Monotonicity requirements 30
5.2.4 The complex floating point result helper functions 30
5.2.5 Basic arithmetic for complex floating point 31
5.2.5.1 Complex floating point comparisons 31
5.2.5.2 Multiplication by the imaginary unit 33
5.2.5.3 The real and imaginary parts of a complex value 34
5.2.5.4 Formation of a complex floating point from two floating point values 34 5.2.5.5 Fundamental complex floating point arithmetic 34
5.2.5.6 Absolute value, phase and signum of complex floating point values 38 5.2.5.7 Floor, round, and ceiling 39
5.2.5.8 Maximum and minimum 39
5.2.6 Complex sign, multiplication, and division 40
5.2.6.1 Complex signum 41
5.2.6.2 Complex multiplication 41
5.2.6.3 Complex division 42
5.2.7 Operations for conversion from polar to Cartesian 43
5.3 Elementary transcendental imaginary and complex floating point operations 44
5.3.1 Operations for exponentiations and logarithms 44
5.3.1.1 Exponentiation of imaginary base to integer power 44
5.3.1.2 Natural exponentiation 45
5.3.1.3 Complex exponentiation of argument base 45

5.3.1.4 Complex square root 46
5.3.1.5 Natural logarithm 47
5.3.2 Operations for radian trigonometric elementary functions 49
5.3.2.1 Radian angle normalisation 49
5.3.2.2 Radian sine 49
5.3.2.3 Radian cosine 50
5.3.2.4 Radian tangent 50
5.3.2.5 Radian cotangent 51
5.3.2.6 Radian secant 52
5.3.2.7 Radian cosecant 52
5.3.2.8 Radian arc sine 53
5.3.2.9 Radian arc cosine 54
5.3.2.10 Radian arc tangent 56
5.3.2.11 Radian arc cotangent 57
5.3.2.12 Radian arc secant 58
5.3.2.13 Radian arc cosecant 59
5.3.3 Operations for hyperbolic elementary functions 60
5.3.3.1 Hyperbolic normalisation 61
5.3.3.2 Hyperbolic sine 61
5.3.3.3 Hyperbolic cosine 61
5.3.3.4 Hyperbolic tangent 61
5.3.3.5 Hyperbolic cotangent 62
5.3.3.6 Hyperbolic secant 62
5.3.3.7 Hyperbolic cosecant 62
5.3.3.8 Inverse hyperbolic sine 62
5.3.3.9 Inverse hyperbolic cosine 63
5.3.3.10 Inverse hyperbolic tangent 63
5.3.3.11 Inverse hyperbolic cotangent 64
5.3.3.12 Inverse hyperbolic secant 64
5.3.3.13 Inverse hyperbolic cosecant 65
5.4 Operations for conversion between imaginary and complex numeric datatypes 65
5.4.1 Integer to complex integer conversions 65
5.4.2 Floating point to complex floating point conversions 66
5.5 Support for imaginary and complex numerals 67

6 Notification 68 6.1 Continuation values 68

7 Relationship with language standards 68 8 Documentation requirements 69 Annex A (normative) Partial conformity 71 A.1 Maximum error relaxation 71

A.2 Extra accuracy requirements relaxation 71
A.3 Relationships to other operations relaxation 72
A.4 Part 1 and part 2 requirements relaxation 72

Annex B (informative) Rationale 73 B.1 Scope 73

B.1.1 Inclusions 73
B.1.2 Exclusions 73
B.2 Conformity 73
B.3 Normative references 74
B.4 Symbols and definitions 74
B.4.1 Symbols 74
B.4.1.1 Sets and intervals 74
B.4.1.2 Operators and relations 74
B.4.1.3 Mathematical functions 74
B.4.1.4 Exceptional values 75
B.4.1.5 Datatypes and special values 75
B.4.1.6 Complex value constructors and complex datatype constructors . 75 B.4.2 Definitions of terms 75
B.5 Specifications for the imaginary and complex datatypes and operations 76
B.5.1 Imaginary and complex integer datatypes and operations 76
B.5.2 Imaginary and complex floating point datatypes and operations 76

B.5.2.1 Maximum error requirements 76
B.5.2.2 Sign requirements 76
B.5.2.3 Maximum error requirements 76
B.5.2.4 Basic arithmetic for complex floating point 77
B.5.3 Elementary transcendental imaginary and complex floating point operations 78 B.5.3.1 Operations for exponentiations and logarithms 78
B.5.3.2 Operations for radian trigonometric elementary functions 78
B.5.3.2.1 Radian angle normalisation 78
B.5.3.2.2 Radian sine 79
B.5.3.2.3 Radian cosine 79
B.5.3.2.4 Radian tangent 79
B.5.3.2.5 Radian cotangent 80
B.5.3.2.6 Radian secant 80
B.5.3.2.7 Radian cosecant 80
B.5.3.2.8 Radian arc sine 80
B.5.3.2.9 Radian arc cosine 81
B.5.3.2.10 Radian arc tangent 81
B.5.3.2.11 Radian arc cotangent 81
B.5.3.2.12 Radian arc secant 81
B.5.3.2.13 Radian arc cosecant 81
B.5.3.3 Operations for hyperbolic elementary functions 82
B.5.3.3.1 Hyperbolic normalisation 82
B.5.3.3.2 Hyperbolic sine 82
B.5.3.3.3 Hyperbolic cosine 82
B.5.3.3.4 Hyperbolic tangent 82
B.5.3.3.5 Hyperbolic cotangent 83
B.5.3.3.6 Hyperbolic secant 83
B.5.3.3.7 Hyperbolic cosecant 83
B.5.3.3.8 Inverse hyperbolic sine 83
B.5.3.3.9 Inverse hyperbolic cosine 83
B.5.3.3.10 Inverse hyperbolic tangent 84
B.5.3.3.11 Inverse hyperbolic cotangent 84
B.5.3.3.12 Inverse hyperbolic secant 84
B.5.3.3.13 Inverse hyperbolic cosecant 84
B.5.4 Operations for conversion between imaginary and complex numeric datatypes 84 B.5.5 Support for imaginary and complex numerals 84
B.6 Notification 84
B.6.1 Continuation values 84
B.7 Relationship with language standards 84
B.8 Documentation requirements 84

Annex C (informative) Example bindings for specific languages 85 C.1 Ada 86

C.2 C 96
C.3 C++ 105
C.4 Fortran 113
C.5 Common Lisp 122