

# ISO/IEC 13751:2001-02 (E)

Information technology\_ - Programming languages, their environments and system software  
interfaces\_ - Programming language Extended\_APL

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