

# ISO/IEC 15909-1:2019 (E)

## Systems and software engineering — High-level Petri nets — Part 1: Concepts, definitions and graphical notation

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