

# ISO/IEC 18031:2011-11 (E)

## Information technology - Security techniques - Random bit generation

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