

# ISO/IEC 15946-1:2008-04 (E)

## Information technology - Security techniques - Cryptographic techniques based on elliptic curves - Part 1: General

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<b>Contents</b>		<b>Page</b>
Foreword .....		iv
Introduction .....		v
<b>1</b>	<b>Scope .....</b>	<b>1</b>
<b>2</b>	<b>Terms and definitions .....</b>	<b>1</b>
<b>3</b>	<b>Symbols .....</b>	<b>2</b>
<b>4</b>	<b>Conventions of fields .....</b>	<b>3</b>
<b>4.1</b>	<b>Finite prime fields <math>F(p)</math> .....</b>	<b>3</b>
<b>4.2</b>	<b>Finite fields <math>F(p^m)</math> .....</b>	<b>3</b>
<b>5</b>	<b>Conventions of elliptic curves .....</b>	<b>4</b>
<b>5.1</b>	<b>Definition of elliptic curves .....</b>	<b>4</b>
<b>5.2</b>	<b>The group law on elliptic curves .....</b>	<b>5</b>
<b>5.3</b>	<b>Cryptographic bilinear map .....</b>	<b>5</b>
<b>6</b>	<b>Conversion functions .....</b>	<b>5</b>
<b>6.1</b>	<b>Octet string / bit string conversion: OS2BSP and BS2OSP .....</b>	<b>5</b>
<b>6.2</b>	<b>Bit string / integer conversion: BS2IP and I2BSP .....</b>	<b>5</b>
<b>6.3</b>	<b>Octet string / integer conversion: OS2IP and I2OSP .....</b>	<b>6</b>
<b>6.4</b>	<b>Finite field element / integer conversion: FE2IPF .....</b>	<b>6</b>
<b>6.5</b>	<b>Octet string / finite field element conversion: OS2FEFP and FE2OSPF .....</b>	<b>6</b>
<b>6.6</b>	<b>Elliptic curve point / octet string conversion: EC2OSPE and OS2ECPE .....</b>	<b>7</b>
<b>6.7</b>	<b>Integer / elliptic curve conversion: I2ECP .....</b>	<b>8</b>
<b>7</b>	<b>Elliptic curve domain parameters and public key .....</b>	<b>8</b>
<b>7.1</b>	<b>Elliptic curve domain parameters over <math>F(q)</math> .....</b>	<b>8</b>
<b>7.2</b>	<b>Elliptic curve key generation .....</b>	<b>9</b>
	<b>Annex A (informative) Background information on finite fields .....</b>	<b>10</b>
<b>A.1</b>	<b>Bit strings .....</b>	<b>10</b>
<b>A.2</b>	<b>Octet strings .....</b>	<b>10</b>
<b>A.3</b>	<b>The finite field <math>F(q)</math> .....</b>	<b>10</b>
	<b>Annex B (informative) Background information on elliptic curves .....</b>	<b>12</b>
<b>B.1</b>	<b>Properties of elliptic curves .....</b>	<b>12</b>
<b>B.2</b>	<b>The group law for elliptic curves <math>E</math> over <math>F(q)</math> with <math>p &gt; 3</math> .....</b>	<b>12</b>
<b>B.3</b>	<b>The group law for elliptic curves over <math>F(2^m)</math> .....</b>	<b>16</b>
<b>B.4</b>	<b>The group law for elliptic curves over <math>F(3^m)</math> .....</b>	<b>17</b>
<b>B.5</b>	<b>The existence condition of an elliptic curve <math>E</math> .....</b>	<b>19</b>
	<b>Annex C (informative) Background information on elliptic curve cryptosystems .....</b>	<b>21</b>
<b>C.1</b>	<b>Definition of cryptographic problems .....</b>	<b>21</b>
<b>C.2</b>	<b>Algorithms to determine discrete logarithms on elliptic curves .....</b>	<b>21</b>
<b>C.3</b>	<b>Scalar multiplication algorithms of elliptic curve points .....</b>	<b>22</b>

C.4	Algorithms to compute pairings .....	24
C.5	Elliptic curve domain parameters and public key validation (optional) .....	25
	Bibliography .....	30