

ISO/IEC Guide 98-5:2026-07 (E)

Guide to the expression of uncertainty in measurement - Part 5: Examples

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