

ISO Guide 98-3:2010-11 (E)

Uncertainty of measurement — Part 3: Guide to the expression of uncertainty in measurement (GUM:1995)

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