

# ISO 10303-104:2000-12 (E)

## Industrial automation systems and integration - Product data representation and exchange - Part 104: Integrated application resource: Finite element analysis

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