ISO 21771-2:2025-12 (E)

Cylindrical involute gears and gear pairs - Part 2: Calculation and measurement of tooth thickness and backlash

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