

# DIN EN 15302:2011-01 (E)

## Railway applications - Method for determining the equivalent conicity (includes Amendment A1:2010)

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