

ISO/IEC 10967-3:2006-05 (E)

Information technology - Language independent arithmetic - Part 3: Complex integer and floating point arithmetic and complex elementary numerical functions

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