

# ISO/IEC Guide 98-4:2012-11 (E)

## Uncertainty of measurement - Part 4: Role of measurement uncertainty in conformity assessment

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