

ISO 10303-104:2000-12 (E)

Industrial automation systems and integration - Product data representation and exchange - Part_104:
Integrated application resource: Finite element analysis

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